

Range Performance Level Descriptors

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8.1.2.A Extend previous knowledge of sets and subsets using a visual representation to describe relationships between sets of real numbers.	Places numbers in a visual representation of the subsets whole numbers, integers, and rational numbers.	 Identifies and justifies visual representations that display relationships among the subsets of real numbers. Classifies rational numbers and describes the relationship among the subsets of real numbers. 	 Classifies real numbers and justifies using attributes of the subsets of real numbers. Generalizes relationships among the subsets of real numbers. 	Describes an error in a visual representation and justifies using attributes of the subsets of real numbers.
8.1.2.B Approximate the value of an irrational number, including π and square roots of numbers less than 225, and locate that rational number approximation on a number line.	 Approximates the value of an irrational square root in a numeric expression. Plots the approximate location of an irrational square root on a number line. Identifies the two consecutive integers between which an irrational number lies. 	 Approximates the value of an irrational number given a point on a number line. Identifies the two rational numbers between which an irrational number lies. 	 Plots the approximate location of an irrational number in terms of π on a number line. 	• Applies an approximated value of an irrational number to real-world contexts.



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8.1.2.C Convert between standard decimal notation and scientific notation.	 Identifies a number written in scientific notation given a number written in standard notation that contains a decimal point, from real-world contexts. Identifies a number written in standard notation given a number written in scientific notation that contains a positive power of 10. 	 Identifies a number written in scientific notation given a whole number written in standard notation from real- world contexts. Identifies a number written in standard notation given a number written in scientific notation that contains a negative power of 10. Determines whether a number written as a product of a rational number and a power of 10 is in scientific notation. 	Creates or writes a number in standard notation given scientific notation.	Creates or writes a number in scientific notation given standard notation.
8.1.2.D Order a set of real numbers arising from mathematical and real-world contexts.	 Compares two positive rational numbers using inequality symbols. Identifies a list of positive real numbers in ascending or descending order. 	 Identifies a value that satisfies a compound inequality involving comparisons of positive real numbers. 	 Identifies or creates an inequality given two real numbers. Orders a set of real numbers in ascending or descending order. 	 Applies ordering a set of real numbers to real-world or mathematical contexts from a variety of numerical representations, such as absolute values, exponents, and irrational numbers written in terms of π.

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8.2.4.A Use similar right triangles to develop an understanding that slope, <i>m</i> , given as the rate comparing the change in <i>y</i> -values to the change in <i>x</i> -values, $(y_2 - y_1)/(x_2 - x_1)$, is the same for any two points (x_1, y_1) and (x_2, y_2) on the same line.	 Identifies coordinates for a point on a line that completes a right triangle that lies on the same line as a given similar triangle, where vertices are shown on a coordinate plane. 	 Identifies or completes a statement comparing the slopes of segments formed by points on the same line using similar right triangles shown on a coordinate plane. 	 Identifies or completes a statement comparing the slopes of segments formed by points on the same line using similar right triangles shown on a coordinate plane and justifies the comparison. Identifies a proportion comparing the numeric change in <i>y</i>-values to the change in <i>x</i>-values to show that the slopes of segments formed by points on the same line are equal, given similar triangles shown on a coordinate plane. 	 Identifies coordinates for a point on a line that completes a right triangle that lies on the same line as a given similar triangle. Creates a proportion comparing side lengths of segments to show that the slopes of segments formed by points on the same line are equal, given similar triangles shown on a coordinate plane.
8.2.4.B Graph proportional relationships, interpreting the unit rate as the slope of the line that models the relationship.	 Identifies a graph of a proportional relationship with a whole number unit rate for which the given rate values can be identified on the graph. 	 Identifies a graph of a proportional relationship with a rational unit rate for which the given rate values can be identified on the graph. 	 Creates a graph of a proportional relationship with a unit rate for which an equivalent rate must be calculated using the given rate values. 	 Creates a graph of a proportional relationship with a unit rate for which an equivalent rate must be calculated using the given fractional rate values.
8.2.4.C Use data from a table or graph to determine the rate of change or slope and <i>y</i> -intercept in mathematical and real-world problems.	 Calculates an integral rate of change given a table where the change in the independent variable is constant. Calculates a slope given a graph with an integral rate of change. 	• Calculates a <i>y</i> -intercept given a table where the change in the independent variable is constant.	• Determines slope and y-intercept given a graph of a linear function.	• Determines rate of change and <i>y</i> -intercept given a table where the change in the independent variable is not constant.

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8.2.5.A Represent linear proportional situations with tables, graphs, and equations in the form of $y = kx$.	Identifies a table or graph representing a proportional relationship given a verbal description including the unit rate of change.	 Identifies a table or graph representing a proportional relationship given a verbal description that does not include the unit rate of change. Identifies an equation representing a proportional relationship given a verbal description including the unit rate of change. Identifies a graph representing a proportional relationship given an equation in the form y = kx. 	 Identifies an equation representing a proportional relationship given a verbal description or a graph that does not include the unit rate of change. Completes a table representing a proportional relationship given corresponding <i>x</i>-values and <i>y</i>- values. Creates a graph representing a proportional relationship given a verbal description. 	Creates a graph representing a proportional relationship given corresponding <i>x</i> -values and <i>y</i> -values.

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8.2.5.B Represent linear non- proportional situations with tables, graphs, and equations in the form of $y = mx + b$, where $b \neq 0$.	• Identifies the equation that represents a linear non- proportional relationship given a verbal description that includes the rate of change and initial value.	 Identifies the equation that represents a linear non- proportional relationship given a table of values where the change in the independent variable is constant. Identifies a table or graph that represents a linear non- proportional situation given a verbal description that includes an integral rate of change and initial value. 	 Completes the equation that represents a linear non- proportional relationship given a table of values where the change in the independent variable is not constant. Identifies a table or graph that represents a linear non- proportional relationship given a verbal description that includes fractional rates of change and initial values. Completes a table that represents a linear non- proportional relationship. 	 Identifies the equation or table that represents a linear non-proportional situation given a verbal description that requires calculation to determine the rate of change or initial value.
8.2.5.E Solve problems involving direct variation.	 Solves problems involving direct variation from real-world contexts in which the given related values are factors of the missing quantity. 	 Solves problems involving direct variation from real- world contexts requiring calculation of the constant of variation. 	 Solves for the dependent variable given mathematical relationships involving direct variation. Completes a table to model direct variation relationships. 	 Solves for the independent variable given mathematical relationships involving direct variation.

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8.2.5.F Distinguish between proportional and non- proportional situations using tables, graphs, and equations in the form $y = kx$ or $y = mx + b$, where $b \neq 0$.	 Identifies a graph of a linear function as having a proportional or non- proportional relationship. 	 Identifies a table that represents a linear function as having a proportional or non-proportional relationship. Identifies an equation that represents a linear function, where the slope is an integer, as a proportional or non-proportional relationship. 	 Identifies a table that represents a linear function as a proportional or non- proportional relationship and justifies the decision using attributes of proportional and non-proportional relationships. Identifies an equation that represents a linear function, where the slope is a rational number, and the relationship is proportional or non- proportional. 	 Identifies an equation that represents a linear function as having a proportional or non- proportional relationship and justifies the decision using attributes of proportional and non-proportional relationships.
8.2.5.G Identify functions using sets of ordered pairs, tables, mappings, and graphs.	 Identifies a function from a set of tables or a set of graphs. 	 Identifies a relation as a function from sets of ordered pairs or a set of mappings. Determines which point to remove from a set of ordered pairs or a table to make the relation a function. 	 Identifies a relation as a function from a combination of representations. Determines which point could be added to a relation so that the relation remains a function. 	 Identifies a relation as a function and justifies the decision using attributes of functions.

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8.2.5.H Identify examples of proportional and non- proportional functions that arise from mathematical and real-world problems.	 Identifies a proportional or non-proportional relationship given a set of graphs. 	 Identifies a proportional or non-proportional relationship given a set of tables containing integer values. Identifies a proportional or non-proportional relationship given a set of real-world situations. 	 Identifies a proportional or non-proportional relationship given a set of equations in slope-intercept form. Describes each linear relationship in a real-world situation as being proportional or non- proportional. 	 Identifies a proportional or non-proportional relationship given a set of tables containing rational values. Identifies a proportional or non-proportional relationship given a set of equations.
8.2.5.I Write an equation in the form $y = mx + b$ to model a linear relationship between two quantities using verbal, numerical, tabular, and graphical representations.	 Identifies an equation in the form y = mx + b that models a real-world situation, given the rate of change and initial value. 	 Identifies an equation in the form y = mx + b that models a real-world situation, given a graph. Identifies an equation in the form y = mx + b that models a linear relationship, given a graph or table. 	 Identifies an equation in the form y = mx + b that models a real-world situation, given a set of independent and dependent values. Creates an equation in the form y = mx + b that models a linear relationship. 	 Writes an equation in the form y = mx + b that models a linear relationship, given a real-world or mathematical context.
8.2.8.A Write one-variable equations or inequalities with variables on both sides that represent problems using rational number coefficients and constants.	• Identifies or completes a one- variable equation with integer coefficients and constants that represents a real-world situation.	 Identifies or completes a one-variable equation with rational number coefficients and constants that represents a real-world situation. Identifies or completes a one-variable inequality with integer coefficients and constants that represents a real-world situation. 	• Identifies or completes a one- variable inequality with rational number coefficients and constants that represents a real-world situation.	• Creates a one-variable equation or inequality with variables on both sides that represents a real-world situation.

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8.2.8.B Write a corresponding real-world problem when given a one-variable equation or inequality with variables on both sides of the equal sign using rational number coefficients and constants.	 Identifies a real-world situation represented by a given one- variable equation with integer coefficients and constants. 	 Identifies a real-world situation represented by a given one-variable equation with rational number coefficients and constants. Completes a real-world situation that can be represented by a given one- variable equation with integer coefficients and constants. Identifies a real-world situation represented by a given one-variable inequality with integer coefficients and constants. 	 Completes a real-world situation that can be represented by a given one- variable inequality with integer coefficients and constants. Identifies a real-world situation that can be represented by a given one- variable inequality with rational number coefficients and constants. 	 Completes a real-world situation that can be represented by a given one- variable equation or inequality with variables on both sides of the equal sign using rational number coefficients and constants.
8.2.8.C Model and solve one- variable equations with variables on both sides of the equal sign that represent mathematical and real-world problems using rational number coefficients and constants.	 Identifies an integer solution given an equation or a pictorial model with variables on both sides of the equal sign and positive coefficients. 	 Identifies a rational solution given an equation or a pictorial model with variables on both sides of the equal sign. Solves an equation that requires combining like terms on one side of the equal sign. Identifies an integer solution for real-world problems that could be represented by an equation with variables on both sides of the equal sign. 	 Solves an equation with an integer solution given an equation or a pictorial model with variables on both sides of the equal sign. Identifies a rational solution for a real-world problem that could be represented by an equation with variables on both sides of the equal sign. 	 Solves an equation with an integer solution given an equation or a pictorial model with variables on both sides of the equal sign, which could involve the application of the distributive property on one side of the equal sign. Models and solves a real-world problem that can be represented by an equation with variables on both sides of the equal sign.



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8.2.9.A Identify and verify the values of x and y that simultaneously satisfy two linear equations in the form $y = mx + b$ from the intersections of the graphed equations.	• Identifies the ordered pair that simultaneously satisfies two linear equations given a graph where the intersection point is in Quadrant I.	 Identifies the ordered pair that simultaneously satisfies two linear equations given a graph. Identifies a statement that describes the ordered pair that simultaneously satisfies two linear equations representing a real-world situation given a graph. 	• Identifies statements that describe each coordinate of the ordered pair that simultaneously satisfies two linear equations representing a real-world situation given a graph.	 Writes the coordinates of the ordered pair that simultaneously satisfies two linear equations given a graph. Writes or completes the statement that describes each coordinate of the ordered pair that simultaneously satisfies two linear equations representing a real-world situation given a graph.
8.3.3.A Generalize that the ratio of corresponding sides of similar shapes are proportional, including a shape and its dilation.	• Determines the proportional relationship of corresponding sides of similar figures, where the orientation of the figures is the same and the sides are labeled with variables and whole numbers.	 Determines the proportional relationship of corresponding sides of similar figures, where the orientation of the figures is the same and the sides are labeled with variables and rational numbers. Determines the proportional relationship of corresponding sides of similar figures, where the figures are reflected and the sides are labeled with variables and numbers. 	 Determines the proportional relationship of corresponding sides of similar figures, where the orientation of the figures is the same and the sides are not labeled with variables or numbers. Determines the proportional relationship of corresponding sides of similar figures, where the figures are rotated and the sides are labeled with variables and numbers. Determines the proportional relationship of corresponding sides of similar figures, where the figures the proportional relationship of corresponding sides of similar figures, where the figures the proportional relationship of corresponding sides of similar figures, where the figures have a common vertex. 	 Determines the proportional relationship of corresponding sides of similar figures, where the figures are reflected or rotated and the sides are not labeled with variables or numbers. Determines the proportional relationship of corresponding sides of similar figures, where the figures have a common side.

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8.3.3.B Compare and contrast the attributes of a shape and its dilation(s) on a coordinate plane.	 Identifies a statement about the effects of a dilation given the scale factor and the graph of the pre-image. 	 Identifies a statement about the effects of a dilation given the graph of the pre-image and an algebraic rule for the dilation. Identifies a statement about the relationship of the side lengths of a dilated image given the scale factor and the graph of the pre-image. 	 level Identifies a statement about the relationship of the side lengths and scale factor of a dilated image given the graph of the image and pre-image. Identifies a statement about the relationship of the angles of a dilated image given the scale factor and the graph of the pre-image. 	 level Identifies a statement about the relationship of the side lengths of a dilated image given the graph of the pre- image and an algebraic rule for the dilation. Identifies a statement about the relationship of the angles of a dilated image given the graph of the pre-image and an algebraic rule for the dilation.

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8.3.3.C Use an algebraic representation to explain the effect of a given positive rational scale factor applied to two-dimensional figures on a coordinate plane with the origin as the center of dilation.	Determines the algebraic representation of a dilation when given a whole number scale factor greater than 1.	• Determines the algebraic representation of a dilation when given a graph or a set of ordered pairs containing the vertices of the image and pre-image, where the scale factor is a whole number or decimal greater than 1.	 Identifies the algebraic representation of a dilation when given a description of the image as being larger or smaller than the pre-image. Determines the algebraic representation of a dilation when given a table containing the vertices of the image and pre-image, where the scale factor is a rational number. Determines the algebraic representation of a dilation when given a graph of the image and pre-image, where the scale factor is a rational number. Determines the algebraic representation of a dilation when given corresponding ordered pairs from the graph of the image and pre-image. Identifies the ordered pair on the graph of a dilation when given the scale factor as a variable. 	• Determines the algebraic representation of a dilation when given the graph of the pre-image and the ordered pair of a corresponding point on the graph of the image.

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8.3.6.A Describe the volume formula <i>V</i> = <i>Bh</i> of a cylinder in terms of its base area and its height.	 Identifies the equation that could be used to determine the area of the base of a cylinder given the volume and height of the cylinder. 	 Identifies the equation that represents the area of the base of a cylinder given the volume and height of the cylinder. Identifies the equation that could be used to determine the height of a cylinder given the volume of the cylinder and the diameter or radius of the base of the cylinder. Identifies the equation or expression that represents the volume of a cylinder given the the height of a cylinder or radius of the base of the cylinder. 	 Creates an equation that represents the area of the base of a cylinder given the volume and height of the cylinder. Identifies the equation that represents the height of a cylinder given the volume and area of the base of the cylinder. Creates an equation or expression that represents the volume of a cylinder given the height of the cylinder and the diameter or radius of the base of the cylinder. 	 Creates an equation that represents the height of a cylinder given the volume of the cylinder and the diameter or radius of the base of the cylinder.
8.3.6.C Use models and diagrams to explain the Pythagorean theorem.	• Identifies the statement that relates the combined areas of the squares that lie on the legs of a right triangle to the area of the square that lies on the hypotenuse.	 Identifies the statement that explains the relationship between the squares that lie on the legs of a right triangle and the square that lies on the hypotenuse. Identifies a set of squares that could be used to create a right triangle, where the side length of each square is given. 	 Determines a set of squares that could be used to create a right triangle, where the side length or area of each square is given. Determines the length of a side in a right triangle when given the lengths of the other sides or the areas of squares that lie on those sides. 	• Determines the area of a square that lies on a side of a right triangle when given the lengths of the other sides or the areas of squares that lie on those sides.

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8.3.7.A Solve problems involving the volume of cylinders, cones, and spheres.	• Approximates the volume of a sphere given the radius of the sphere.	 Approximates the volume of a sphere given the diameter of the sphere. Approximates the volume of a cylinder given the height of the cylinder and the diameter or radius of the base of the cylinder. Approximates the volume of a cone given the height of the cone and the diameter or radius of the base of the cone. 	 Determines the volume of a sphere, in terms of π, given the radius or diameter of the sphere. Determines the volume of a cylinder, in terms of π, given the height of the cylinder and the diameter or radius of the base of the cylinder. Determines the volume of a cone, in terms of π, given the height of the cone and the diameter or radius of the base of the cone. Approximates the radius of the base of a cylinder given the height and approximate volume of the cylinder. Approximates the height of a cylinder given the diameter or radius of the base of a cylinder given the height and approximate volume of the cylinder. Approximates the radius of the base of a cone given the height and approximate volume of the cylinder. Approximates the radius of the base of a cone given the height and approximate volume of the cylinder. Approximates the radius of the base of a cone given the height and approximate volume of the cone. Approximates the height of a cone given the height and approximate volume of the cone. Approximates the height of a cone given the height and approximate volume of the cone. 	 Determines the radius of the base of a cylinder given the height and volume of the cylinder. Determines the height of a cylinder given the volume of the cylinder, in terms of π, and the diameter or radius of the base of the cylinder. Determines the radius of the base of a cone given the height and volume of the cone, in terms of π. Determines the height of a cone given the height of a cone given the volume of the cone, in terms of π. Determines the height of a cone given the volume of the cone, in terms of π. Determines the height of a cone given the volume of the cone, in terms of π, and the diameter or radius of the base of the cone. Determines the volume of composite three-dimensional shapes given the radius or diameter and the height.

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8.3.7.B Use previous knowledge of surface area to make connections to the formulas for lateral and total surface area and determine solutions for problems involving rectangular prisms, triangular prisms, and cylinders.	 Determines the height of a triangular prism given the perimeter of the base and the lateral surface area of the prism. Determines the height of a rectangular prism given the perimeter of the base and the total surface area of the prism. 	 Approximates the total surface area of a cylinder given the height of the cylinder and the diameter or radius of the base of the cylinder. Approximates the lateral surface area of a cylinder given the height of the cylinder and the diameter or radius of the base of the cylinder. Determines the total surface area of a rectangular prism given the dimensions of the prism. 	 level Determines the lateral surface area of a triangular prism given the dimensions of the base and the height of the prism. Determines the height of a triangular prism given the dimensions of the base and the lateral surface area of the prism. Determines the total surface area of a cylinder, in terms of π, given the height of the cylinder and the diameter or radius of the base of the cylinder. Determines the lateral surface area of a cylinder, in terms of π, given the height of the cylinder and the diameter or radius of the base of the cylinder and the diameter or radius of the base of the cylinder and the diameter or radius of the base of the cylinder. Determines the height of a cylinder given the lateral surface area of the cylinder and the diameter or radius of the base of the cylinder. Determines the radius of a cylinder given the lateral surface area and the height of the cylinder. 	 level Determines the total surface area of a triangular prism given the dimensions of the base and the height of the prism. Determines the height of a rectangular prism given the total surface area and the dimensions of the base of the prism.

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8.3.7.C Use the Pythagorean theorem and its converse to solve problems.	 level Identifies the length of the hypotenuse or a leg of a right triangle when given a diagram labeled with the lengths of the other two sides. 	 level Identifies the length of the hypotenuse or a leg of a right triangle when given the lengths of the other two sides. Identifies the length of a diagonal of a rectangle when given a diagram labeled with the length and width of the rectangle. Identifies whether a set of measurements could or could not be the side lengths of a right triangle. Labels a missing side length of a right triangle when given a diagram with some of its dimensions. 	 level Identifies an equation that proves that a quadrilateral is a rectangle when given the measures of the length, width, and diagonal of the quadrilateral. Classifies a triangle as either a right triangle or not a right triangle when given the side lengths. Identifies the perimeter of a right triangle when given a diagram labeled with the lengths of two sides. 	 level Calculates the length of the hypotenuse or a leg of a right triangle when given the lengths of the other two sides. Identifies the length, width, or the length of a diagonal of a rectangle when given the other two dimensions. Determines the side length of a quadrilateral when given a diagram with some of it dimensions and justifies the calculation using the Pythagorean theorem.
8.3.7.D Determine the distance between two points on a coordinate plane using the Pythagorean theorem.	• Identifies the distance between two points when given a graph of the two points, where the two points are in the same quadrant.	• Identifies the distance between two points when given a graph of the two points.	 Identifies the distance between two points when given a graph of one point and a description of the location of the second point in relation to the first point. Identifies the length of a segment when given the graph of a non-horizontal, non-vertical segment. 	 Calculates the distance between two points when given two ordered pairs.



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8.3.8.D Use informal arguments to establish facts about the angle sum and exterior angle of triangles, the angles created when parallel lines are cut by a transversal, and the angle-angle criterion for similarity of triangles.	Identifies a statement that describes a missing angle measure when given a partially labeled diagram and three labeled diagrams of an angle relationship.	• Determines an expression or equation that models an angle relationship when given a partially labeled diagram and three labeled diagrams of an angle relationship.	• Completes a statement that describes an angle relationship when given a partially labeled diagram and three labeled diagrams of an angle relationship.	• Determines missing angle measures when given a partially labeled diagram and three labeled diagrams of an angle relationship.
8.3.10.A Generalize the properties of orientation and congruence of rotations, reflections, translations, and dilations of two-dimensional shapes on a coordinate plane.	 Identifies the statement that describes the effect of a rotation, reflection, or translation in terms of side lengths, angle measures, and figure orientation when given the graph of the image and pre-image. 	 Identifies the statement that describes the effect of a rotation, reflection, or translation in terms of side lengths, angle measures, or figure orientation when given the graph or a description of the pre-image. 	 Identifies the statement that describes the effect of a transformation in terms of side lengths, angle measures, or figure orientation when given an algebraic representation or a graph of the pre-image. 	 Identifies a transformation when given effects of the transformation on a figure.
8.3.10.B Differentiate between transformations that preserve congruence and those that do not.	Identifies the transformation that does not preserve congruence, where the scale factor of the dilation is an integer.	 Identifies the transformation that does not preserve congruence, where the scale factor of the dilation is a rational number. Identifies the transformation that preserves congruence. 	Identifies the algebraic representation of a transformation that does or does not preserve congruence.	 Identifies the verbal description of a transformation that does or does not preserve congruence. Identifies the vertices of an image transformed in a way that does not preserve congruence, when given the vertices or graph of the pre- image.

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8.3.10.C Explain the effect of translations, reflections over the <i>x</i> - or <i>y</i> -axis, and rotations limited to 90°, 180°, 270°, and 360° as applied to two-dimensional shapes on a coordinate plane using an algebraic representation.	• Determines the algebraic representation of a translation when given a verbal description of the translation, where both the <i>x</i> -coordinate and the <i>y</i> -coordinate are translated.	 Determines the algebraic representation of a translation when given a verbal description of the translation, where only the <i>x</i>- coordinate or the <i>y</i>-coordinate is translated. Determines the algebraic representation of a reflection when given a verbal description of the reflection. Determines the algebraic representation of a rotation of 180° about the origin when given a verbal description of the rotation. 	 Determines the algebraic representation of a translation when given the graph of the image and pre- image. Determines the algebraic representation of a reflection when given the graph of the image and pre-image. Determines the algebraic representation of a clockwise rotation about the origin when given a verbal description of the rotation. Identifies a transformation as a translation or reflection when given the algebraic representation of the transformation. 	 Determines the algebraic representation of a clockwise rotation about the origin when given the graph of the image and pre-image. Determines the algebraic representation of a counterclockwise rotation about the origin when given a verbal description of the rotation. Determines the algebraic representation of a counterclockwise rotation about the origin when given the graph of the image and pre-image. Identifies a transformation as a rotation when given the algebraic representation of the transformation.

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8.3.10.D Model the effect on linear and area measurements of dilated two-dimensional shapes.	• Identifies the statement that relates the perimeter of an image to the perimeter of the pre-image when given an integer scale factor.	• Identifies the statement that relates the perimeter of an image to the perimeter of the pre-image when given a rational number scale factor.	 Identifies the statement that relates the area of an image to the area of the pre-image when given an integer scale factor. Identifies an expression that represents the perimeter of an image when given the dimensions or perimeter of the pre-image. Determines the ratio of the perimeters of the image and pre-image. 	 Identifies the statement that relates the area of an image to the area of the pre-image when given a rational number scale factor. Identifies an expression that represents the area of an image when given the dimensions or area of the pre-image. Determines the ratio of the areas of the image and pre- image.
8.4.5.C Contrast bivariate sets of data that suggest a linear relationship with bivariate sets of data that do not suggest a linear relationship from a graphical representation.	• Identifies the graph that shows a linear relationship when given bivariate sets of data graphed on a coordinate grid.	 Identifies the graph that shows a non-linear relationship when given bivariate sets of data graphed on a coordinate grid. Determines a set of points that could be added to the graph of a bivariate set of data so that the relationship remains linear. 	• Describes the relationship of a bivariate set of data graphed on a coordinate grid as linear.	• Describes the relationship of a bivariate set of data graphed on a coordinate grid as non-linear.

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8.4.5.D Use a trend line that approximates the linear relationship between bivariate sets of data to make predictions.	• Determines the value of the response variable when given the value of an explanatory variable of a bivariate set of data with a strong positive linear relationship.	• Determines the value of the response variable when given the value of an explanatory variable of a bivariate set of data with a positive linear relationship.	 Determines the value of the response variable when given the value of an explanatory variable of a bivariate set of data with a negative linear relationship. Determines the value of the explanatory variable when given the value of a response variable of a bivariate set of data with a positive linear relationship. 	• Determines the value of the explanatory variable when given the value of a response variable of a bivariate set of data with a negative linear relationship.
8.4.11.A Construct a scatterplot and describe the observed data to address questions of association such as linear, non- linear, and no association between bivariate data.	 Identifies or completes the statement that describes the relationship of a bivariate set of data graphed on a coordinate grid where the graph shows a positive linear association. 	 Identifies or completes the statement that describes the relationship of a bivariate set of data graphed on a coordinate grid, where the graph shows a negative linear association. Identifies the graph that shows a negative or positive linear association when given a bivariate set of data graphed on a coordinate grid. 	 Identifies or completes the statement that describes the relationship of a bivariate set of data graphed on a coordinate grid, where the graph shows no apparent association. 	 Identifies or completes the statement that describes the relationship of a bivariate set of data graphed on a coordinate grid, where the graph shows a non-linear association. Constructs a scatterplot that shows the relationship of a bivariate set of data such as linear, non-linear, and no association.

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8.4.11.B Determine the mean absolute deviation and use this quantity as a measure of the average distance data are from the mean using a data set of no more than 10 data points.	 Calculates the mean absolute deviation from a data set that contains no more than 5 data values, where the mean and the mean absolute deviation are whole numbers. 	 Calculates the mean absolute deviation from a data set that contains no more than 5 data values, where the mean and the mean absolute deviation are rational numbers. 	• Calculates the mean absolute deviation from a data set that contains no more than 10 data values, where the mean is a whole number and the mean absolute deviation is a rational number.	 Calculates the mean absolute deviation from a data set that contains no more than 10 data values, where the mean and the mean absolute deviation are rational numbers.
8.4.12.A Solve real-world problems comparing how interest rate and loan length affect the cost of credit.	 Identifies the difference between the total amounts of interest paid for two different loans when given the loan length and interest rate for each loan, where the interest rate is a whole number percent. 	 Identifies the difference between the total amounts of interest paid for two different loans when given the loan length and interest rate for each loan, where the interest rate is a decimal percent. Completes statements identifying the cost of credit for two different loans when given the loan lengths and interest rates. Identifies a loan with the greatest cost of credit when given a set of loan lengths and interest rates. 	• Completes statements comparing the cost of credit for two different loans when given the loan lengths and interest rates.	• Calculates the difference between the total amounts of interest paid for two different loans when given the loan length and interest rate for each loan.

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8.4.12.C Explain how small amounts of money invested regularly, including money saved for college and retirement, grow over time.	 Identifies how the balance in an account grows, given general information about the type of activity in the account. 	• Determines the effect of regular deposits and interest on the balance of an account when given a table showing the activity in the account over a length of time.	• Determines the effect of regular deposits and interest on the balance of an account when given quantitative information about the activity in the account.	• Describes how the interest rate is applied to an account, given a table showing the activity in the account over a length of time.
8.4.12.D Calculate and compare simple interest and compound interest earnings.	• Calculates the simple interest earnings on an investment given a principal amount, a length of time, and an interest rate.	• Calculates the total amount of an investment that earns compound interest, given a principal amount, a length of time, and an interest rate.	 Calculates compound interest earnings on an investment given a principal amount, a length of time, and an interest rate. Calculates the total amount of an investment for a simple interest investment given a principal amount, a length of time, and an interest rate. 	 Calculates the difference between investment values given a principal amount, investment types, lengths of time, and interest rates. Completes a statement identifying or comparing the interest earnings or investment values for two different investments given a principal amount, investment types, lengths of time, and interest rates.
8.4.12.G Estimate the cost of a two-year and four-year college education, including family contribution, and devise a periodic savings plan for accumulating the money needed to contribute to the total cost of attendance for at least the first year of college.	 Determines the amount of money to save on a regular basis to pay for one year of college, given the cost of tuition per year at the college. 	• Determines the amount of money to save on a regular basis to pay for one year of college, where tuition will be partly paid with a scholarship or previous savings, given the cost of tuition per year at the college.	 Determines the amount of money to save on a regular basis for one or two years of college, where tuition will be partly paid with a scholarship or previous savings, and the total cost of attending the college must be calculated. 	 Determines the amount of money to save on a regular basis for two or more years of college, where tuition will be partly paid with a scholarship or previous savings, and the total cost of attending the college must be calculated.