Math, Grade 2 (IMRA)

Subject: Mathematics

Grade: 02 Expectations: 50 Breakouts: 158

(a) Introduction.

- 1. The desire to achieve educational excellence is the driving force behind the Texas essential knowledge and skills for mathematics, guided by the college and career readiness standards. By embedding statistics, probability, and finance, while focusing on computational thinking, mathematical fluency, and solid understanding, Texas will lead the way in mathematics education and prepare all Texas students for the challenges they will face in the 21st century.
- 2. The process standards describe ways in which students are expected to engage in the content. The placement of the process standards at the beginning of the knowledge and skills listed for each grade and course is intentional. The process standards weave the other knowledge and skills together so that students may be successful problem solvers and use mathematics efficiently and effectively in daily life. The process standards are integrated at every grade level and course. When possible, students will apply mathematics to problems arising in everyday life, society, and the workplace. Students will use a problem-solving model that incorporates analyzing given information, formulating a plan or strategy, determining a solution, justifying the solution, and evaluating the problem-solving process and the reasonableness of the solution. Students will select appropriate tools such as real objects, manipulatives, algorithms, paper and pencil, and technology and techniques such as mental math, estimation, number sense, and generalization and abstraction to solve problems. Students will effectively communicate mathematical ideas, reasoning, and their implications using multiple representations such as symbols, diagrams, graphs, computer programs, and language. Students will use mathematical relationships to generate solutions and make connections and predictions. Students will analyze mathematical relationships to connect and communicate mathematical ideas. Students will display, explain, or justify mathematical ideas and arguments using precise mathematical language in written or oral communication.
- 3. For students to become fluent in mathematics, students must develop a robust sense of number. The National Research Council's report, "Adding It Up," defines procedural fluency as "skill in carrying out procedures flexibly, accurately, efficiently, and appropriately." As students develop procedural fluency, they must also realize that true problem solving may take time, effort, and perseverance. Students in Grade 2 are expected to perform their work without the use of calculators.
- 4. The primary focal areas in Grade 2 are making comparisons within the base-10 place value system, solving problems with addition and subtraction within 1,000, and building foundations for multiplication.
 - a. Students develop an understanding of the base-10 place value system and place value concepts. The students' understanding of base-10 place value includes ideas of counting in units and multiples of thousands, hundreds, tens, and ones and a grasp of number relationships, which students demonstrate in a variety of ways.
 - Students identify situations in which addition and subtraction are useful to solve problems. Students develop a
 variety of strategies to use efficient, accurate, and generalizable methods to add and subtract multi-digit whole
 numbers.
 - c. Students use the relationship between skip counting and equal groups of objects to represent the addition or subtraction of equivalent sets, which builds a strong foundation for multiplication and division.
- 5. Statements that contain the word "including" reference content that must be mastered, while those containing the phrase "such as" are intended as possible illustrative examples.
- (b) Knowledge and Skills Statements

- (1) Mathematical process standards. The student uses mathematical processes to acquire and demonstrate mathematical understanding. The student is expected to:
 - (A) apply mathematics to problems arising in everyday life, society, and the workplace;
 - (i) apply mathematics to problems arising in everyday life
 - (ii) apply mathematics to problems arising in society
 - (iii) apply mathematics to problems arising in the workplace
 - (B) use a problem-solving model that incorporates analyzing given information, formulating a plan or strategy, determining a solution, justifying the solution, and evaluating the problem-solving process and the reasonableness of the solution;
 - (i) use a problem-solving model that incorporates analyzing given information, formulating a plan or strategy, determining a solution, justifying the solution, and evaluating the problem-solving process
 - (ii) use a problem-solving model that incorporates analyzing given information, formulating a plan or strategy, determining a solution, justifying the solution, and evaluating the reasonableness of the solution
 - (C) select tools, including real objects, manipulatives, paper and pencil, and technology as appropriate, and techniques, including mental math, estimation, and number sense as appropriate, to solve problems;
 - (i) select tools, including real objects as appropriate, to solve problems
 - (ii) select tools, including manipulatives as appropriate, to solve problems
 - (iii) select tools, including paper and pencil as appropriate, to solve problems
 - (iv) select tools, including technology as appropriate, to solve problems
 - (v) select techniques, including mental math as appropriate, to solve problems
 - (vi) select techniques, including estimation as appropriate, to solve problems
 - (vii) select techniques, including number sense as appropriate, to solve problems
 - (D) communicate mathematical ideas, reasoning, and their implications using multiple representations, including symbols, diagrams, graphs, and language as appropriate;
 - (i) communicate mathematical ideas using multiple representations, including symbols as appropriate
 - (ii) communicate mathematical ideas using multiple representations, including diagrams as appropriate
 - (iii) communicate mathematical ideas using multiple representations, including graphs as appropriate
 - (iv) communicate mathematical ideas using multiple representations, including language as appropriate
 - (v) communicate mathematical reasoning using multiple representations, including symbols as appropriate
 - (vi) communicate mathematical reasoning using multiple representations, including diagrams as appropriate
 - (vii) communicate mathematical reasoning using multiple representations, including graphs as appropriate
 - (viii) communicate mathematical reasoning using multiple representations, including language as appropriate
 - (ix) communicate [mathematical ideas'] implications using multiple representations, including symbols as appropriate
 - (x) communicate [mathematical ideas'] implications using multiple representations, including diagrams as appropriate

- (xi) communicate [mathematical ideas'] implications using multiple representations, including graphs as appropriate
- (xii) communicate [mathematical ideas'] implications using multiple representations, including language as appropriate
- (xiii) communicate [mathematical reasoning's] implications using multiple representations, including symbols as appropriate
- (xiv) communicate [mathematical reasoning's] implications using multiple representations, including diagrams as appropriate
- (xv) communicate [mathematical reasoning's] implications using multiple representations, including graphs as appropriate
- (xvi) communicate [mathematical reasoning's] implications using multiple representations, including language as appropriate
- (E) create and use representations to organize, record, and communicate mathematical ideas;
 - (i) create representations to organize mathematical ideas
 - (ii) use representations to organize mathematical ideas
 - (iii) create representations to record mathematical ideas
 - (iv) use representations to record mathematical ideas
 - (v) create representations to communicate mathematical ideas
 - (vi) use representations to communicate mathematical ideas
- (F) analyze mathematical relationships to connect and communicate mathematical ideas; and
 - (i) analyze mathematical relationships to connect mathematical ideas
 - (ii) analyze mathematical relationships to communicate mathematical ideas
- (G) display, explain, and justify mathematical ideas and arguments using precise mathematical language in written or oral communication.
 - (i) display mathematical ideas using precise mathematical language in written or oral communication
 - (ii) display mathematical arguments using precise mathematical language in written or oral communication
 - (iii) explain mathematical ideas using precise mathematical language in written or oral communication
 - (iv) explain mathematical arguments using precise mathematical language in written or oral communication
 - (v) justify mathematical ideas using precise mathematical language in written or oral communication
 - (vi) justify mathematical arguments using precise mathematical language in written or oral communication
- (2) Number and operations. The student applies mathematical process standards to understand how to represent and compare whole numbers, the relative position and magnitude of whole numbers, and relationships within the numeration system related to place value. The student is expected to:
 - (A) use concrete and pictorial models to compose and decompose numbers up to 1,200 in more than one way as a sum of so many thousands, hundreds, tens, and ones;
 - (i) use concrete models to compose numbers up to 1,200 in more than one way as a sum of so many thousands, hundreds, tens, and ones

- (ii) use concrete models to decompose numbers up to 1,200 in more than one way as a sum of so many thousands, hundreds, tens, and ones
- (iii) use pictorial models to compose numbers up to 1,200 in more than one way as a sum of so many thousands, hundreds, tens, and ones
- (iv) use pictorial models to decompose numbers up to 1,200 in more than one way as a sum of so many thousands, hundreds, tens, and ones
- (B) use standard, word, and expanded forms to represent numbers up to 1,200;
 - (i) use standard forms to represent numbers up to 1,200
 - (ii) use word forms to represent numbers up to 1,200
 - (iii) use expanded forms to represent numbers up to 1,200
- (C) generate a number that is greater than or less than a given whole number up to 1,200;
 - (i) generate a number that is greater than or less than a given whole number up to 1,200
- (D) use place value to compare and order whole numbers up to 1,200 using comparative language, numbers, and symbols (>, <, or =);
 - (i) use place value to compare whole numbers up to 1,200 using comparative language
 - (ii) use place value to order whole numbers up to 1,200 using comparative language
 - (iii) use place value to compare whole numbers up to 1,200 using numbers
 - (iv) use place value to order whole numbers up to 1,200 using numbers
 - (v) use place value to compare whole numbers up to 1,200 using symbols (>, <, or =)
 - (vi) use place value to order whole numbers up to 1,200 using symbols (>, <, or =)
- (E) locate the position of a given whole number on an open number line; and
 - (i) locate the position of a given whole number on an open number line
- (F) name the whole number that corresponds to a specific point on a number line.
 - (i) name the whole number that corresponds to a specific point on a number line
- (3) Number and operations. The student applies mathematical process standards to recognize and represent fractional units and communicates how they are used to name parts of a whole. The student is expected to:
 - (A) partition objects into equal parts and name the parts, including halves, fourths, and eighths, using words;
 - (i) partition objects into equal parts, including halves
 - (ii) partition objects into equal parts, including fourths
 - (iii) partition objects into equal parts including eighths
 - (iv) name the parts using words, including halves
 - (v) name the parts using words, including fourths
 - (vi) name the parts using words, including eighths
 - (B) explain that the more fractional parts used to make a whole, the smaller the part; and the fewer the fractional parts, the larger the part;

- (i) explain that the more fractional parts used to make a whole, the smaller the part
- (ii) explain that the fewer the fractional parts [used to make a whole], the larger the part
- (C) use concrete models to count fractional parts beyond one whole using words and recognize how many parts it takes to equal one whole; and
 - (i) use concrete models to count fractional parts beyond one whole using words
 - (ii) recognize how many parts it takes to equal one whole
- (D) identify examples and non-examples of halves, fourths, and eighths.
 - (i) identify examples of halves
 - (ii) identify examples of fourths
 - (iii) identify examples of eighths
 - (iv) identify non-examples of halves
 - (v) identify non-examples of fourths
 - (vi) identify non-examples of eighths
- (4) Number and operations. The student applies mathematical process standards to develop and use strategies and methods for whole number computations in order to solve addition and subtraction problems with efficiency and accuracy. The student is expected to:
 - (A) recall basic facts to add and subtract within 20 with automaticity;
 - (i) recall basic facts to add within 20 with automaticity
 - (ii) recall basic facts to subtract within 20 with automaticity
 - (B) add up to four two-digit numbers and subtract two-digit numbers using mental strategies and algorithms based on knowledge of place value and properties of operations;
 - (i) add up to four two-digit numbers using mental strategies based on knowledge of place value
 - (ii) add up to four two-digit numbers using mental strategies based on knowledge of properties of operations
 - (iii) add up to four two-digit numbers using algorithms based on knowledge of place value
 - (iv) add up to four two-digit numbers using algorithms based on knowledge of properties of operations
 - (v) subtract two-digit numbers using mental strategies based on knowledge of place value
 - (vi) subtract two-digit numbers using mental strategies based on knowledge of properties of operations
 - (vii) subtract two-digit numbers using algorithms based on knowledge of place value
 - (viii) subtract two-digit numbers using algorithms based on knowledge of properties of operations
 - (C) solve one-step and multi-step word problems involving addition and subtraction within 1,000 using a variety of strategies based on place value, including algorithms; and
 - (i) solve one-step word problems involving addition within 1,000 using a variety of strategies based on place value, including algorithms
 - (ii) solve one-step word problems involving subtraction within 1,000 using a variety of strategies based on place value, including algorithms

- (iii) solve multi-step word problems involving addition within 1,000 using a variety of strategies based on place value, including algorithms
- (iv) solve multi-step word problems involving subtraction within 1,000 using a variety of strategies based on place value, including algorithms
- (v) solve multi-step word problems involving addition and subtraction within 1,000 using a variety of strategies based on place value, including algorithms
- (D) generate and solve problem situations for a given mathematical number sentence involving addition and subtraction of whole numbers within 1,000.
 - (i) generate problem situations for a given mathematical number sentence involving addition of whole numbers within 1,000
 - (ii) generate problem situations for a given mathematical number sentence involving subtraction of whole numbers within 1,000
 - (iii) solve problem situations for a given mathematical number sentence involving addition of whole numbers within 1,000
 - (iv) solve problem situations for a given mathematical number sentence involving subtraction of whole numbers within 1,000
- (5) Number and operations. The student applies mathematical process standards to determine the value of coins in order to solve monetary transactions. The student is expected to:
 - (A) determine the value of a collection of coins up to one dollar; and
 - (i) determine the value of a collection of coins up to one dollar
 - (B) use the cent symbol, dollar sign, and the decimal point to name the value of a collection of coins.
 - (i) use the cent symbol to name the value of a collection of coins
 - (ii) use the dollar sign and the decimal point to name the value of a collection of coins
- (6) Number and operations. The student applies mathematical process standards to connect repeated addition and subtraction to multiplication and division situations that involve equal groupings and shares. The student is expected to:
 - (A) model, create, and describe contextual multiplication situations in which equivalent sets of concrete objects are joined; and
 - (i) model contextual multiplication situations in which equivalent sets of concrete objects are joined
 - (ii) create contextual multiplication situations in which equivalent sets of concrete objects are joined
 - (iii) describe contextual multiplication situations in which equivalent sets of concrete objects are joined
 - (B) model, create, and describe contextual division situations in which a set of concrete objects is separated into equivalent sets.
 - (i) model contextual division situations in which a set of concrete objects is separated into equivalent sets
 - (ii) create contextual division situations in which a set of concrete objects is separated into equivalent sets
 - (iii) describe contextual division situations in which a set of concrete objects is separated into equivalent sets
- (7) Algebraic reasoning. The student applies mathematical process standards to identify and apply number patterns within properties of numbers and operations in order to describe relationships. The student is expected to:
 - (A) determine whether a number up to 40 is even or odd using pairings of objects to represent the number;

- (i) determine whether a number up to 40 is even or odd using pairings of objects to represent the number
- (B) use an understanding of place value to determine the number that is 10 or 100 more or less than a given number up to 1,200; and
 - (i) use an understanding of place value to determine the number that is 10 or 100 more or less than a given number up to 1,200
- (C) represent and solve addition and subtraction word problems where unknowns may be any one of the terms in the problem.
 - (i) represent addition word problems where unknowns may be any one of the terms in the problem
 - (ii) represent subtraction word problems where unknowns may be any one of the terms in the problem
 - (iii) solve addition word problems where unknowns may be any one of the terms in the problem
 - (iv) solve subtraction word problems where unknowns may be any one of the terms in the problem
- (8) Geometry and measurement. The student applies mathematical process standards to analyze attributes of two-dimensional shapes and three-dimensional solids to develop generalizations about their properties. The student is expected to:
 - (A) create two-dimensional shapes based on given attributes, including number of sides and vertices;
 - (i) create two-dimensional shapes based on given attributes, including number of sides
 - (ii) create two-dimensional shapes based on given attributes, including number of vertices
 - (B) classify and sort three-dimensional solids, including spheres, cones, cylinders, rectangular prisms (including cubes as special rectangular prisms), and triangular prisms, based on attributes using formal geometric language;
 - (i) classify three-dimensional solids, including spheres, based on attributes using formal geometric language
 - (ii) classify three-dimensional solids, including cones, based on attributes using formal geometric language
 - (iii) classify three-dimensional solids, including cylinders, based on attributes using formal geometric language
 - (iv) classify three-dimensional solids, including rectangular prisms (including cubes as special rectangular prisms), based on attributes using formal geometric language
 - (v) classify three-dimensional solids, including triangular prisms, based on attributes using formal geometric language
 - (vi) sort three-dimensional solids, including spheres, based on attributes using formal geometric language
 - (vii) sort three-dimensional solids, including cones, based on attributes using formal geometric language
 - (viii) sort three-dimensional solids, including cylinders, based on attributes using formal geometric language
 - (ix) sort three-dimensional solids, including rectangular prisms (including cubes as special rectangular prisms), based on attributes using formal geometric language
 - (x) sort three-dimensional solids, including triangular prisms, based on attributes using formal geometric language
 - (C) classify and sort polygons with 12 or fewer sides according to attributes, including identifying the number of sides and number of vertices;
 - (i) classify polygons with 12 or fewer sides according to attributes, including identifying the number of sides
 - (ii) classify polygons with 12 or fewer sides according to attributes, including identifying the number of vertices

- (iii) sort polygons with 12 or fewer sides according to attributes, including identifying the number of sides
- (iv) sort polygons with 12 or fewer sides according to attributes, including identifying the number of vertices
- (D) compose two-dimensional shapes and three-dimensional solids with given properties or attributes; and
 - (i) compose two-dimensional shapes with given properties or attributes
 - (ii) compose three-dimensional solids with given properties or attributes
- (E) decompose two-dimensional shapes such as cutting out a square from a rectangle, dividing a shape in half, or partitioning a rectangle into identical triangles and identify the resulting geometric parts.
 - (i) decompose two-dimensional shapes
 - (ii) identify the resulting geometric parts
- (9) Geometry and measurement. The student applies mathematical process standards to select and use units to describe length, area, and time. The student is expected to:
 - (A) find the length of objects using concrete models for standard units of length;
 - (i) find the length of objects using concrete models for standard units of length
 - (B) describe the inverse relationship between the size of the unit and the number of units needed to equal the length of an object;
 - (i) describe the inverse relationship between the size of the unit and the number of units needed to equal the length of an object
 - (C) represent whole numbers as distances from any given location on a number line;
 - (i) represent whole numbers as distances from any given location on a number line
 - (D) determine the length of an object to the nearest marked unit using rulers, yardsticks, meter sticks, or measuring tapes;
 - (i) determine the length of an object to the nearest marked unit using rulers, yardsticks, meter sticks, or measuring tapes
 - (E) determine a solution to a problem involving length, including estimating lengths;
 - (i) determine a solution to a problem involving length, including estimating lengths
 - (F) use concrete models of square units to find the area of a rectangle by covering it with no gaps or overlaps, counting to find the total number of square units, and describing the measurement using a number and the unit; and
 - (i) use concrete models of square units to find the area of a rectangle by covering it with no gaps or overlaps, counting to find the total number of square units, and describing the measurement using a number and the unit
 - (G) read and write time to the nearest one-minute increment using analog and digital clocks and distinguish between a.m. and p.m.
 - (i) read time to the nearest one-minute increment using analog clocks
 - (ii) write time to the nearest one-minute increment using analog clocks
 - (iii) read time to the nearest one-minute increment using digital clocks
 - (iv) write time to the nearest one-minute increment using digital clocks

- (v) distinguish between a.m. and p.m.
- (10) Data analysis. The student applies mathematical process standards to organize data to make it useful for interpreting information and solving problems. The student is expected to:
 - (A) explain that the length of a bar in a bar graph or the number of pictures in a pictograph represents the number of data points for a given category;
 - (i) explain that the length of a bar in a bar graph or the number of pictures in a pictograph represents the number of data points for a given category
 - (B) organize a collection of data with up to four categories using pictographs and bar graphs with intervals of one or more;
 - (i) organize a collection of data with up to four categories using pictographs with intervals of one or more
 - (ii) organize a collection of data with up to four categories using bar graphs with intervals of one or more
 - (C) write and solve one-step word problems involving addition or subtraction using data represented within pictographs and bar graphs with intervals of one; and
 - (i) write one-step word problems involving addition or subtraction using data represented within pictographs with intervals of one
 - (ii) write one-step word problems involving addition or subtraction using data represented within bar graphs with intervals of one
 - (iii) solve one-step word problems involving addition or subtraction using data represented within pictographs with intervals of one
 - (iv) solve one-step word problems involving addition or subtraction using data represented within bar graphs with intervals of one
 - (D) draw conclusions and make predictions from information in a graph.
 - (i) draw conclusions from information in a graph
 - (ii) make predictions from information in a graph
- (11) Personal financial literacy. The student applies mathematical process standards to manage one's financial resources effectively for lifetime financial security. The student is expected to:
 - (A) calculate how money saved can accumulate into a larger amount over time;
 - (i) calculate how money saved can accumulate into a larger amount over time
 - (B) explain that saving is an alternative to spending;
 - (i) explain that saving is an alternative to spending
 - (C) distinguish between a deposit and a withdrawal;
 - (i) distinguish between a deposit and a withdrawal
 - (D) identify examples of borrowing and distinguish between responsible and irresponsible borrowing;
 - (i) identify examples of borrowing
 - (ii) distinguish between responsible and irresponsible borrowing
 - (E) identify examples of lending and use concepts of benefits and costs to evaluate lending decisions; and
 - (i) identify examples of lending

- (ii) use concepts of benefits to evaluate lending decisions
- (iii) use concepts of costs to evaluate lending decisions
- (F) differentiate between producers and consumers and calculate the cost to produce a simple item.
 - (i) differentiate between producers and consumers
 - (ii) calculate the cost to produce a simple item